

# Exploring the singlet scalar dark matter from direct detections and neutrino signals via its annihilation in the Sun

Wan-Lei Guo and Yue-Liang Wu, arXiv:1103.5606

Wan-lei Guo

郭万磊

中国科学院理论物理研究所

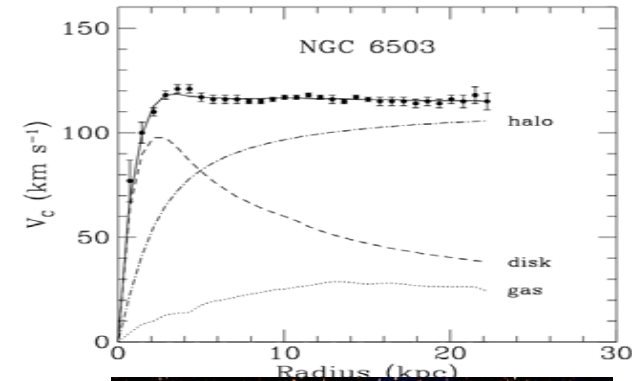
2011兩岸粒子物理與宇宙學研討會  
Cross Strait Meeting on Particle Physics and Cosmology  
2011-04-03

- ❖ The DM annihilation in the Sun
- ❖ Direct detections in two singlet scalar DM (SSDM) models:
  - ❑ SSDM-SM **Z2**
  - ❑ SSDM-2HBDM **P and CP**
- ❖ Neutrino signals in the Super-K and IceCube
- ❖ Summary

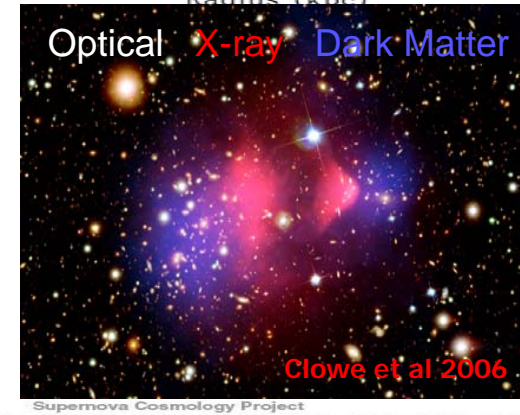
# Evidences for dark matter

3

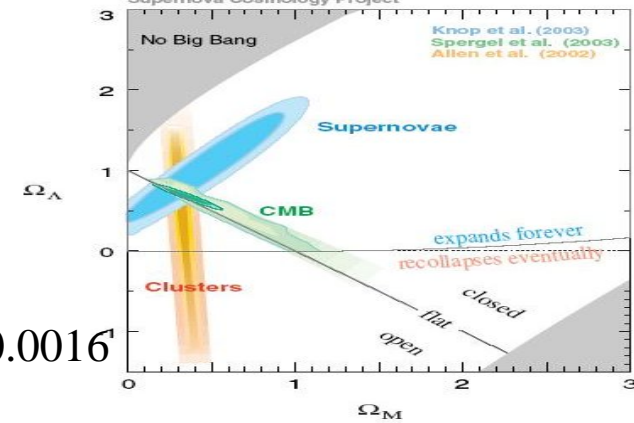
(1) The galactic scale:  
Flat rotation curves



(2) The scale of galaxy clusters:  
The velocity of galaxies in clusters  
The X-rays trace the hot gas  
The gravitational lensing



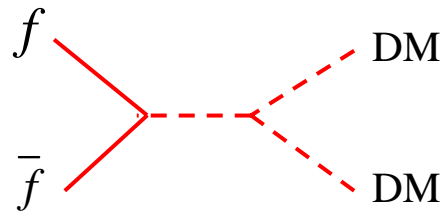
(3) The cosmological scale:  
Large scale structure  
CMB



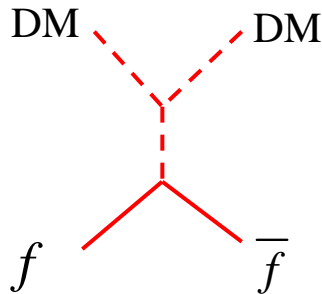
**WMAP 7:**  $\Omega_\Lambda = 0.728^{+0.015}_{-0.016}$ ;  $\Omega_{DM} = 0.227 \pm 0.014$ ;  $\Omega_b = 0.0456 \pm 0.0016$

# Dark matter searches

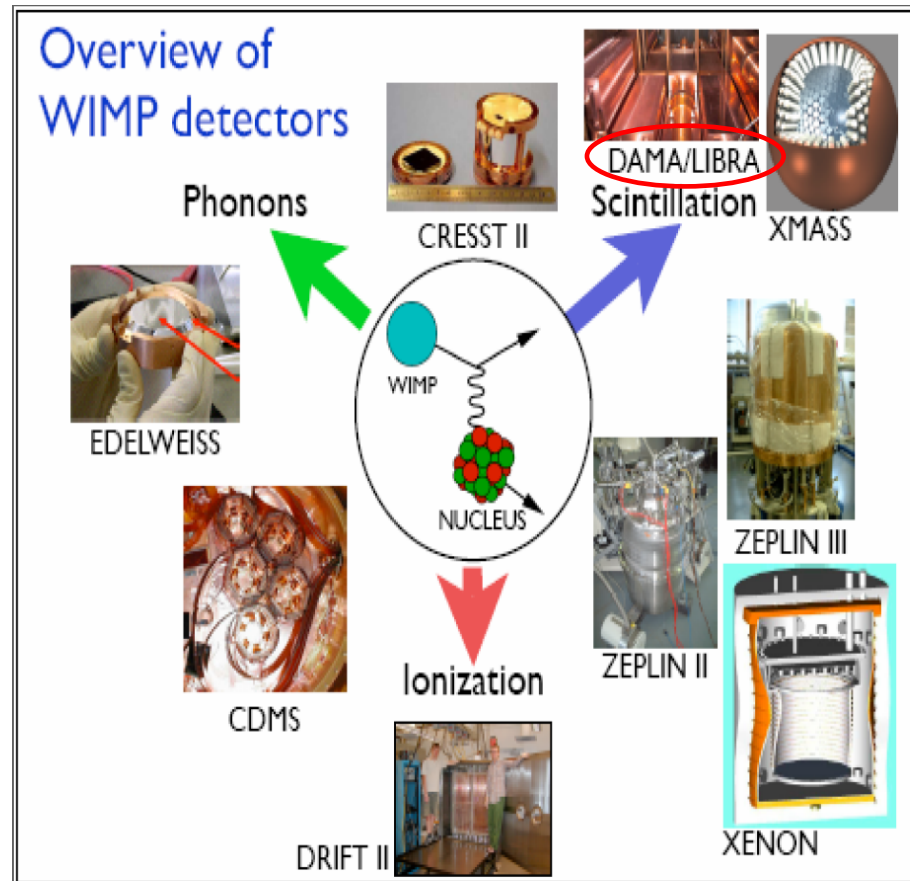
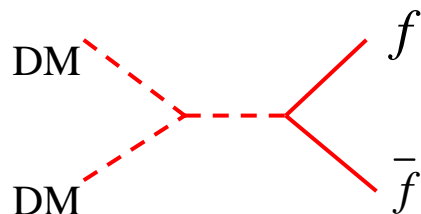
## (1) Collider search:



## (2) Direct search:



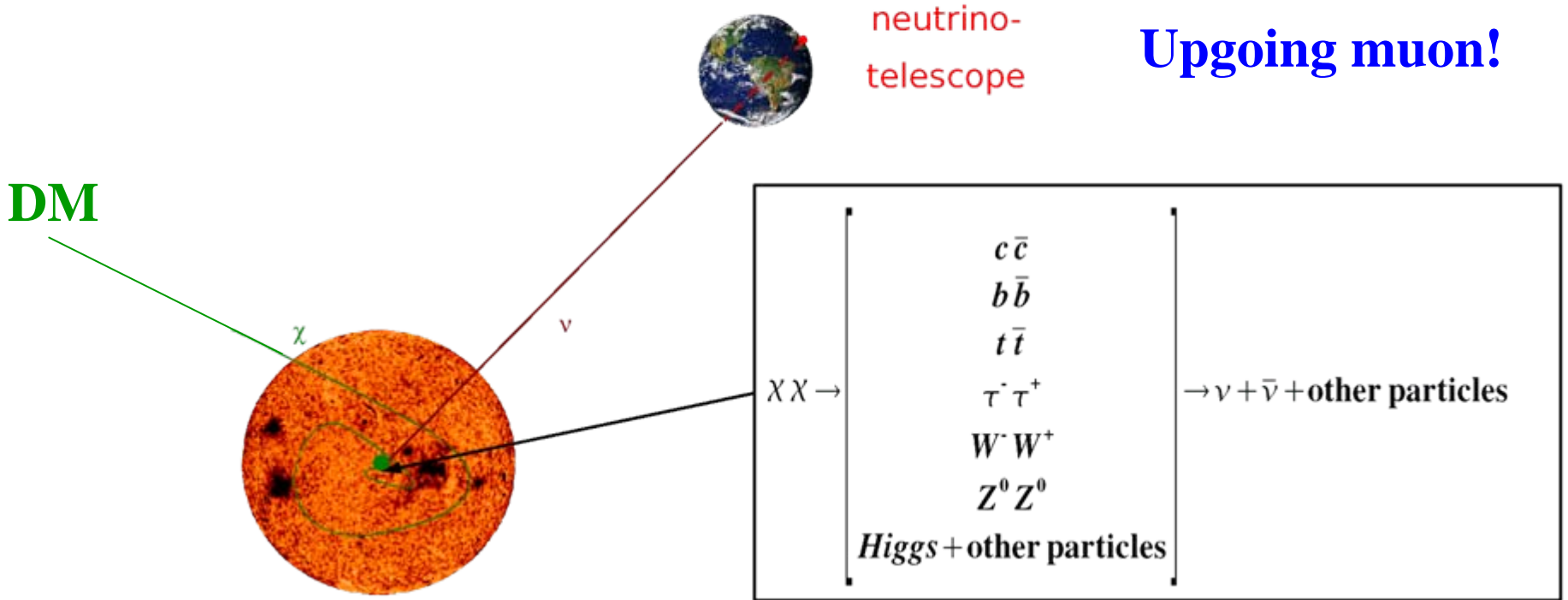
## (3) Indirect search:



## Annihilation productions:

Gamma rays, Neutrinos, electrons, Positrons  
Protons and antiprotons etc.

# DM capture and annihilation in the Sun 5



DM elastic scattering  
in the Sun



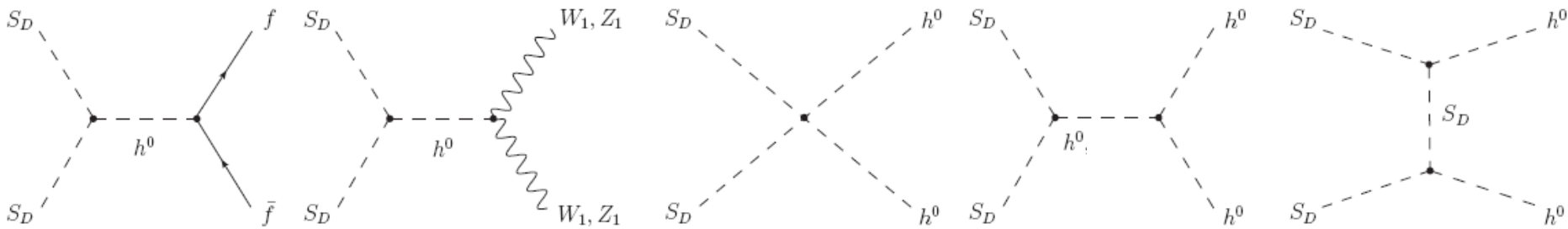
DM is captured  
when  $V_{\text{DM}} < V_{\text{esc}}$



Instantaneous  
thermalization

# Real singlet scalar DM model as an extension of SM 6

$$\mathcal{L} = \mathcal{L}_{\text{SM}} + \frac{1}{2} \partial_\mu S \partial^\mu S - \frac{m_0^2}{2} S^2 - \frac{\lambda_S}{4} S^4 - \lambda S^2 H^\dagger H \quad \mathbf{Z}_2$$



$$\hat{\sigma}_{ff} = \sum_f \frac{\lambda^2 m_f^2}{\pi} \frac{1}{(s - m_h^2)^2 + m_h^2 \Gamma_h^2} \frac{(s - 4m_f^2)^{1.5}}{\sqrt{s}},$$

$$\hat{\sigma}_{ZZ} = \frac{\lambda^2}{4\pi} \frac{s^2}{(s - m_h^2)^2 + m_h^2 \Gamma_h^2} \sqrt{1 - \frac{4m_Z^2}{s}} \left( 1 - \frac{4m_Z^2}{s} + \frac{12m_Z^4}{s^2} \right),$$

$$\hat{\sigma}_{WW} = \frac{\lambda^2}{2\pi} \frac{s^2}{(s - m_h^2)^2 + m_h^2 \Gamma_h^2} \sqrt{1 - \frac{4m_W^2}{s}} \left( 1 - \frac{4m_W^2}{s} + \frac{12m_W^4}{s^2} \right),$$

$$\hat{\sigma}_{hh} = \frac{\lambda^2}{4\pi} \sqrt{1 - \frac{4m_h^2}{s}} \left[ \left( \frac{s + 2m_h^2}{s - m_h^2} \right)^2 - \frac{16\lambda v_{\text{EW}}^2}{s - 2m_h^2} \frac{s + 2m_h^2}{s - m_h^2} F(\xi) + \frac{32\lambda^2 v_{\text{EW}}^4}{(s - 2m_h^2)^2} \left( \frac{1}{1 - \xi_h^2} + F(\xi) \right) \right]$$

**3 parameters**

# Dark matter relic density

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## Boltzmann Equation:

$$\frac{dY}{dx} = -\frac{x \mathbf{s}(x)}{H} \langle \sigma v \rangle (Y^2 - Y_{EQ}^2), \quad (11)$$

where  $Y \equiv n/\mathbf{s}(x)$  denotes the dark matter number density. The entropy density  $\mathbf{s}(x)$  and the Hubble parameter  $H$  evaluated at  $x = 1$  are given by

$$\mathbf{s}(x) = \frac{2\pi^2 g_*}{45} \frac{m^3}{x^3}; \quad (12)$$

$$H = \sqrt{\frac{4\pi^3 g_*}{45}} \frac{m^2}{M_{PL}}, \quad (13)$$

where  $M_{PL} \simeq 1.22 \times 10^{19}$  GeV is the Planck energy.  $g_*$

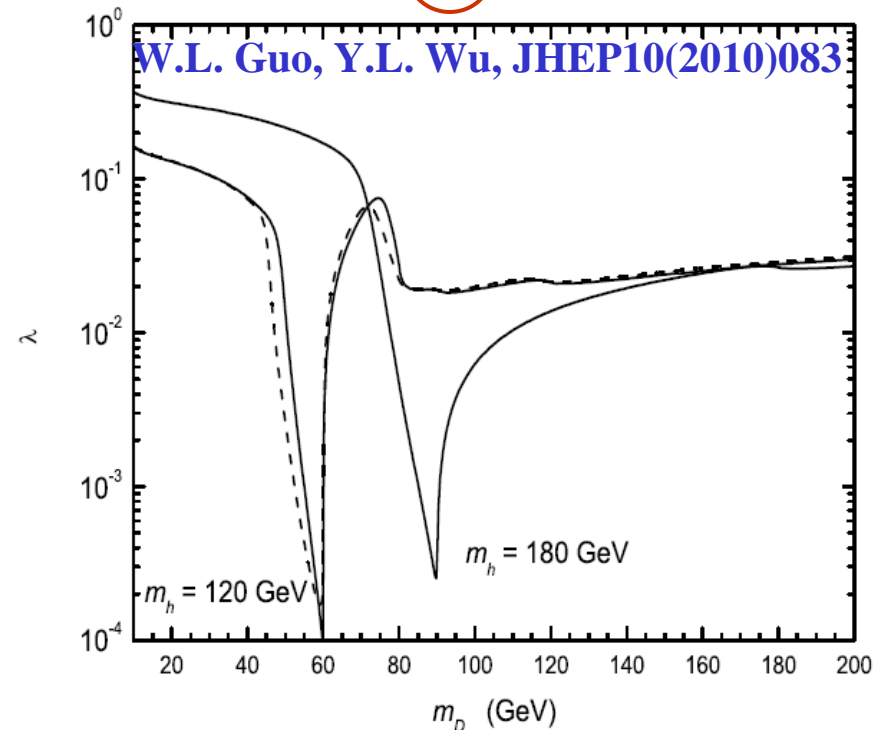
$$\Omega_D h^2 = 2.74 \times 10^8 \frac{m}{\text{GeV}} Y_0$$

$$0.1088 \leq \Omega_D h^2 \leq 0.1158$$

$$\langle \sigma v \rangle = \frac{1}{n_{EQ}^2} \frac{m_D}{64\pi^4 x} \int_{4m_D^2}^{\infty} \hat{\sigma}(s) \sqrt{s} K_1\left(\frac{x\sqrt{s}}{m_D}\right) ds,$$

$$n_{EQ} = \frac{g_i}{2\pi^2} \frac{m_D^3}{x} K_2(x),$$

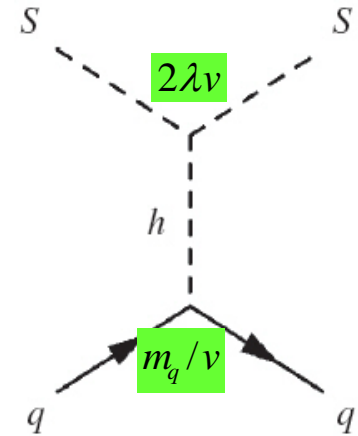
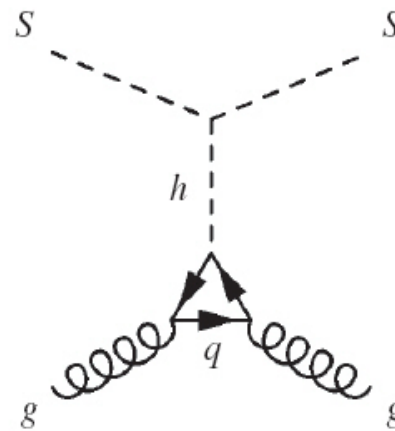
$$\hat{\sigma}(s) \in \hat{\sigma} g_i^2 \sqrt{1 - \frac{4m_D^2}{s}},$$



## WIMP-nucleon cross section:

$$\sigma_n^{\text{SI}} \approx \frac{\lambda^2}{\pi} f^2 \frac{m_n^2}{m_h^4 m_D^2} \left( \frac{m_D m_n}{m_D + m_n} \right)^2$$

$$f = (7/9) \sum_{q=u,d,s} f_{Tq}^p + 2/9$$



**J. Ellis, et. al., PRD81,085004,(2010) [0912.3137]**

$$f \approx 0.56 \pm 0.17$$

**J. Giedt, et. al., PRL103,201802,(2009) [0907.4177]**

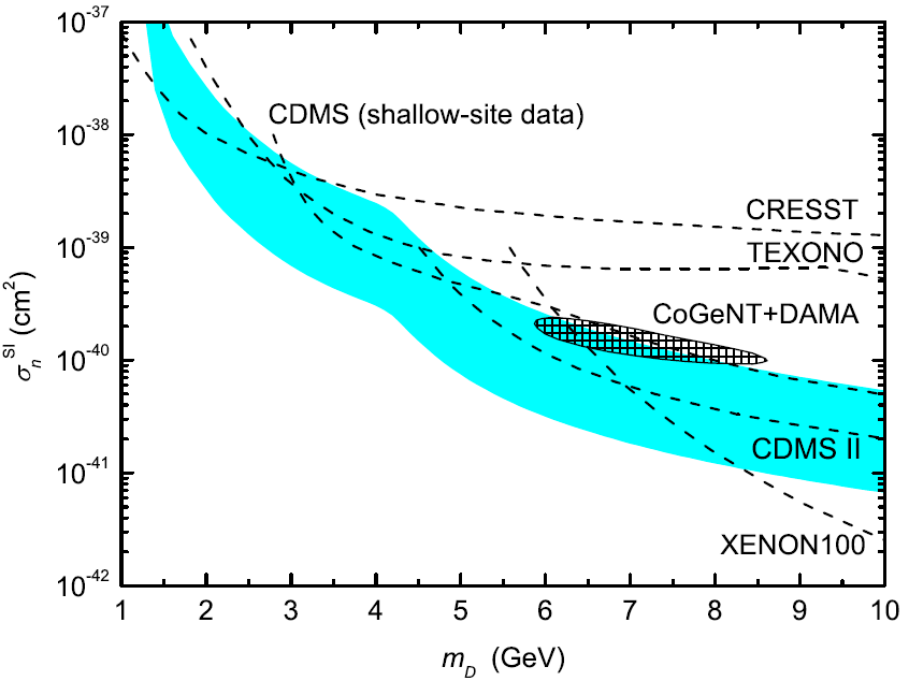
$$f \approx 0.29 \pm 0.03$$

$$0.26 \leq f \leq 0.73$$

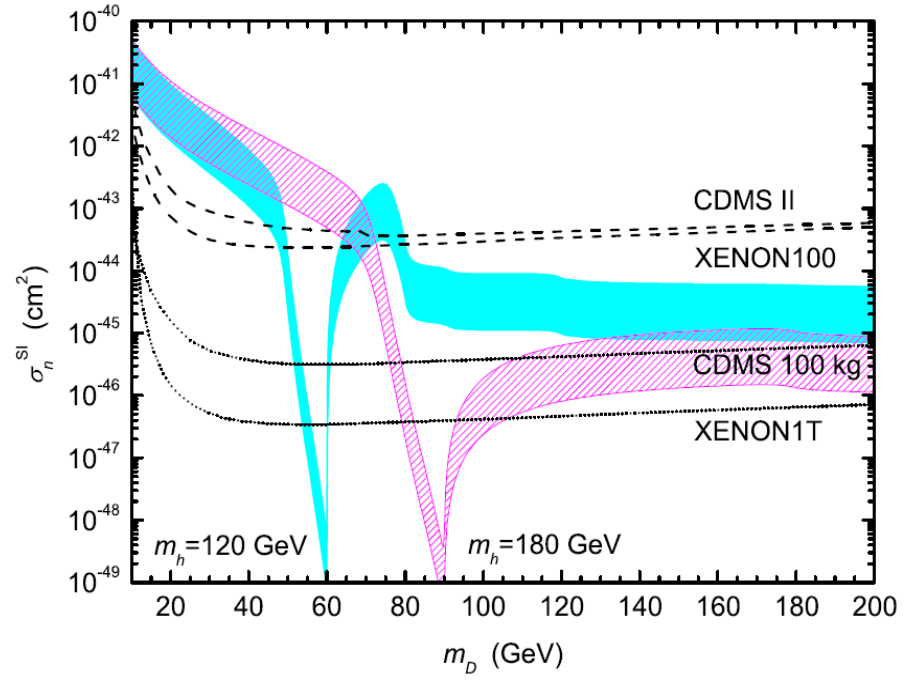


# Constraints from the DM direct search

W.L. Guo, Y.L. Wu, arXiv:1103.5606



**CoGeNT+DAMA**  
Exclude  $f > 0.63$



**Two excluded regions!**  
**Future experiments**

# Complex SSDM model as an extension of 2HBDM:SSDM-2HBDM

Y.L. Wu and Y.F. Zhou, 0709.0042; 0711.3891

## Left-right symmetric two Higgs bidoublet model:

$$SU(2)_L \times SU(2)_R \times U(1)_{B-L}$$

right-handed gauge bosons,  
right-handed neutrinos and

$$\phi = \begin{pmatrix} \phi_1^0 & \phi_1^+ \\ \phi_2^- & \phi_2^0 \end{pmatrix}, \quad \chi = \begin{pmatrix} \chi_1^0 & \chi_1^+ \\ \chi_2^- & \chi_2^0 \end{pmatrix}$$

$$\Delta_{L,R} = \begin{pmatrix} \delta_{L,R}^+ / \sqrt{2} & \delta_{L,R}^{++} \\ \delta_{L,R}^0 & -\delta_{L,R}^+ / \sqrt{2} \end{pmatrix}$$

W.L. Guo, Y.L. Wu and Y.F. Zhou, PRD82,095004(2010)

If we introduce a gauge singlet  $S = \frac{S_\sigma + iS_D}{\sqrt{2}}$  with  $S \xrightarrow{CP} S^*$  and  $S^* \xrightarrow{CP} S$

|                 | $P$             | $CP$              |  | $P$ | $CP$ |  | $P$ | $CP$ |
|-----------------|-----------------|-------------------|--|-----|------|--|-----|------|
| $\phi$          | $\phi^\dagger$  | $\phi^*$          | $S + S^*$  | +   | +    | $S - S^*$  | +   | -    |
| $\chi$          | $\chi^\dagger$  | $\chi^*$          | $SS^*$   | +   | +    | $\text{Tr}(\phi^\dagger \phi)$                                     | +   | +    |
| $\Delta_{L(R)}$ | $\Delta_{R(L)}$ | $\Delta_{L(R)}^*$ | $\text{Tr}(\phi^\dagger \tilde{\phi} + \tilde{\phi}^\dagger \phi)$ | +   | +    | $\text{Tr}(\phi^\dagger \tilde{\phi} - \tilde{\phi}^\dagger \phi)$ | -   | -    |
| $S$             | $S$             | $S^*$             | $\text{Tr}(\Delta_L^\dagger \Delta_L + \Delta_R^\dagger \Delta_R)$ | +   | +    | $\text{Tr}(\Delta_L^\dagger \Delta_L - \Delta_R^\dagger \Delta_R)$ | -   | +    |

Unique way!

# A light DM mass and DM annihilation

**For WIMP:**  $1 \text{ GeV} \leq m_D \leq 1 \text{ TeV}$

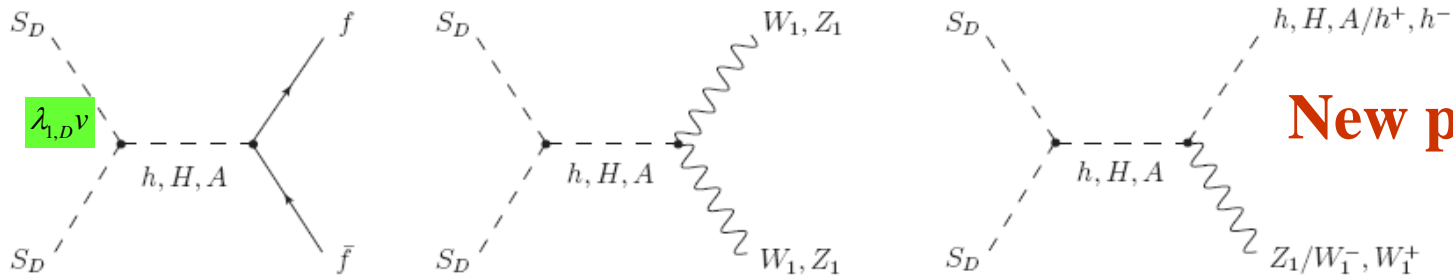
$v_R \sim 10 \text{ TeV} \Rightarrow$  An approximate global symmetry:

$$S \xrightarrow{U(1)} e^{iq} S \Rightarrow \text{light DM mass}$$

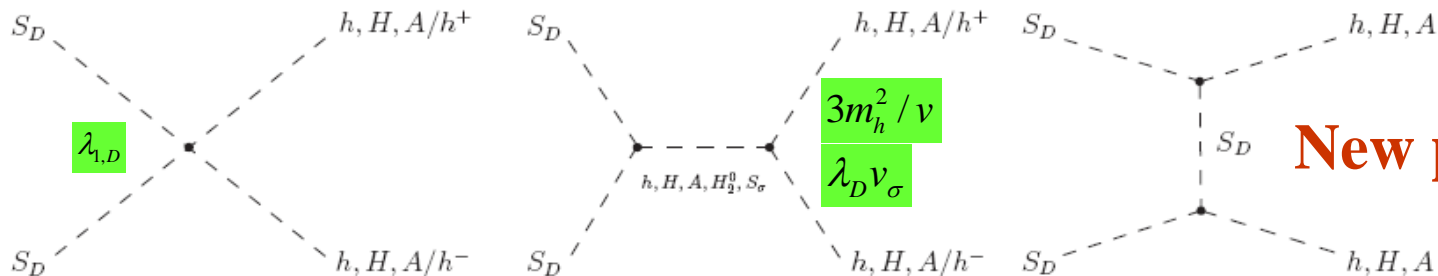
**Higgs potential related to the Singlet:**

$$\mathcal{V}_S = -\mu_D^2 S S^* + \lambda_D (S S^*)^2 + \sum_{i=1}^3 \lambda_{i,D} S S^* O_i - \frac{m_D^2}{4} (S - S^*)^2$$

$$O_1 = \text{Tr}(\phi^\dagger \phi), O_2 = \text{Tr}(\phi^\dagger \tilde{\phi} + \tilde{\phi}^\dagger \phi) \text{ and } O_3 = \text{Tr}(\Delta_L^\dagger \Delta_L + \Delta_R^\dagger \Delta_R).$$



**New processes**



**New products**

# Yukawa couplings in the SSDM-2HBDM

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$$\phi = \begin{pmatrix} \phi_1^0 & \phi_1^+ \\ \phi_2^- & \phi_2^0 \end{pmatrix}, \chi = \begin{pmatrix} \chi_1^0 & \chi_1^+ \\ \chi_2^- & \chi_2^0 \end{pmatrix} \xrightarrow[\kappa_2 \sim w_2 \sim 0]{\text{SSB}} \phi' = \begin{pmatrix} \frac{h_1+v}{\sqrt{2}} & \phi_1'^+ \\ 0 & \phi_2'^0 \end{pmatrix}, \chi' = \begin{pmatrix} \frac{h_2+ih_3}{\sqrt{2}} & \chi_1'^+ \\ h^- & \chi_2'^0 \end{pmatrix}$$

## Light Higgs mixing:

$$\begin{pmatrix} h_1 \\ h_2 \\ h_3 \end{pmatrix} = \begin{pmatrix} c_x c_z & s_x c_z & s_z \\ -c_x s_y s_z - s_x c_y & -s_x s_y s_z + c_x c_y & s_y c_z \\ -c_x c_y s_z + s_x s_y & -s_x c_y s_z - c_x s_y & c_y c_z \end{pmatrix} \begin{pmatrix} h \\ H \\ A \end{pmatrix} \rightarrow \begin{matrix} \text{Case I: } \theta_x=60^\circ, \theta_y=60^\circ, \theta_z=150^\circ \\ \text{Case II: } \theta_x=30^\circ, \theta_y=0^\circ, \theta_z=0^\circ \\ \text{Case III: } \theta_x=0^\circ, \theta_y=90^\circ, \theta_z=75^\circ \end{matrix}$$

## Yukawa interactions:

$$-\mathcal{L}_Y = \overline{Q}_L (Y^\phi \phi' + \tilde{Y}^\phi \tilde{\phi}' + Y^\chi \chi' + \tilde{Y}^\chi \tilde{\chi}') Q_R + h.c., \quad \text{Complex symmetric!}$$

$$-\mathcal{L}_{LH} = \frac{h_1 + v_{\text{EW}}}{\sqrt{2}} (\overline{u}'_L Y^\phi u'_R + \overline{d}'_L \tilde{Y}^\phi d'_R) + \frac{h_2 + ih_3}{\sqrt{2}} \overline{u}'_L Y^\chi u'_R + \frac{h_2 - ih_3}{\sqrt{2}} \overline{d}'_L \tilde{Y}^\chi d'_R + h.c.$$

$$\Rightarrow Y_{qq}^{\phi'} = \sqrt{2} m_q / v_{\text{EW}} \text{ and } \tilde{Y}_{qq}^{\phi'} = \sqrt{2} m_q / v_{\text{EW}}$$

$$Y_{qq}^{\chi'} = R Y_{qq}^{\phi'} \text{ and } \tilde{Y}_{qq}^{\chi'} = R \tilde{Y}_{qq}^{\phi'}$$

Diagonal!

$$R_q = 1$$

$$R_l = 1 \ 0$$

## WIMP-nucleon cross section:

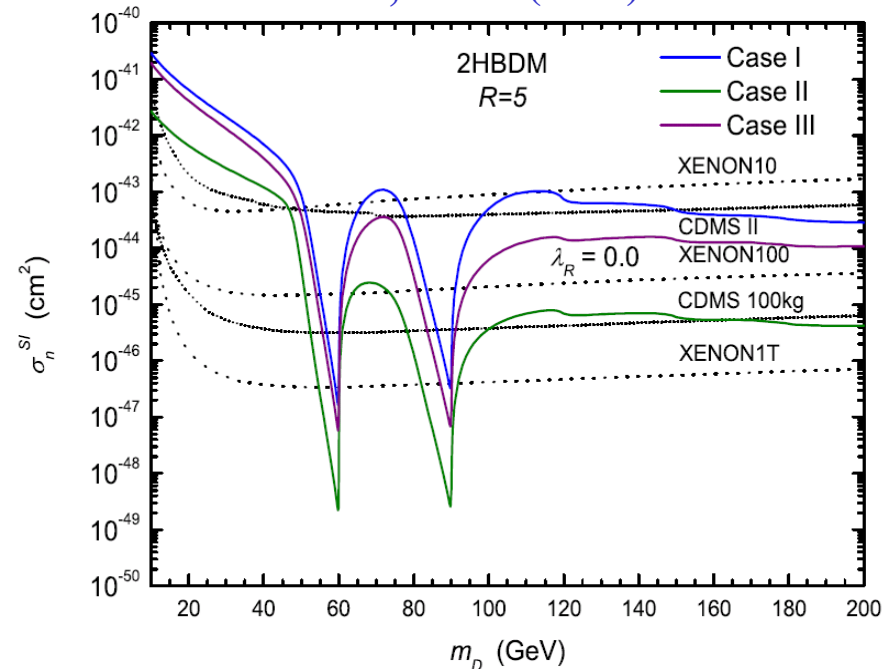
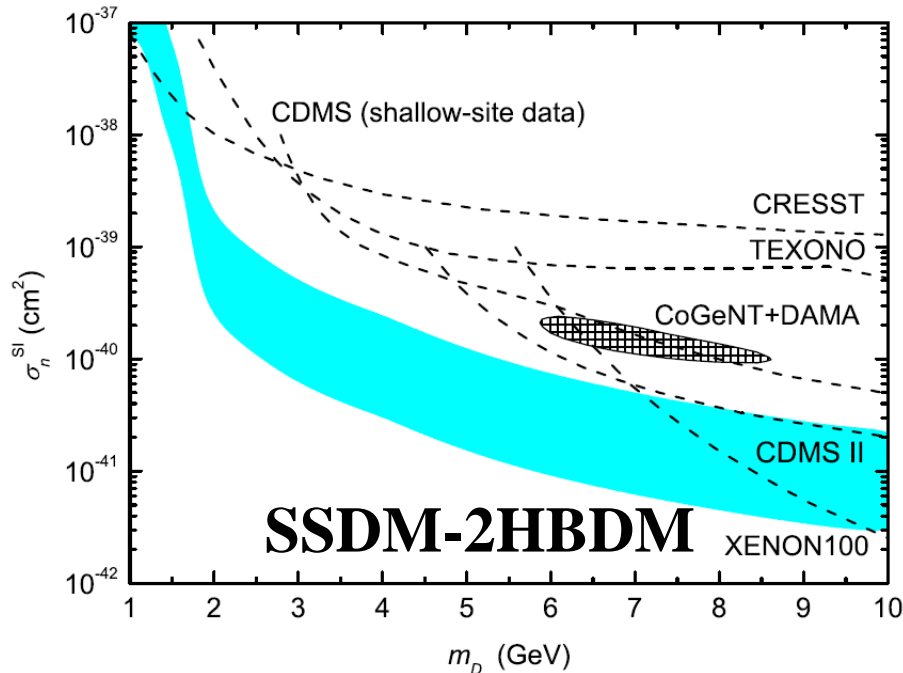
$$\sigma_n^{SI} \approx \frac{\lambda_{1,D}^2}{4\pi} f^2 \frac{m_n^2}{m_D^2} \left( \frac{m_D m_n}{m_D + m_n} \right)^2 \left( \frac{f_1}{m_h^2} + \frac{f_3}{m_H^2} + \frac{f_5}{m_A^2} \right)^2$$

$$f_1 = c_x c_z - R c_y s_x - R c_x s_y s_z,$$

$$f_3 = R c_x c_y + c_z s_x - R s_x s_y s_z,$$

$$f_5 = R s_y c_z + s_z,$$

W.L. Guo, Y.L. Wu, Y.F. Zhou,  
PRD82,095004(2010)



# DM capture and annihilation rates

## The evolution of DM number in the Sun:

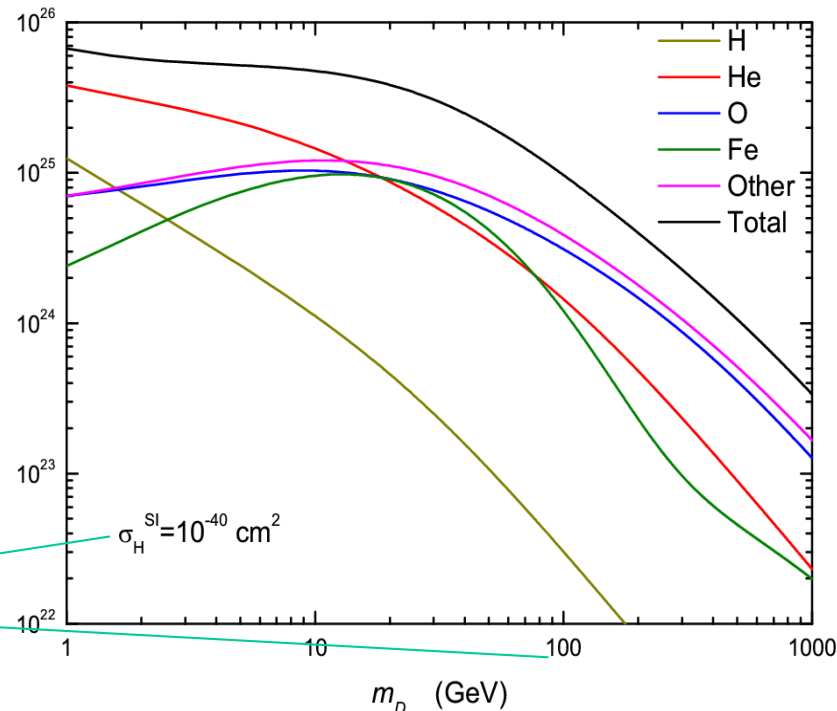
$$\dot{N} = C_{\odot} - C_E N - C_A N^2$$

$$C_{\odot} \approx 4.8 \times 10^{24} \text{s}^{-1} \frac{\rho_{\text{DM}}}{0.3 \text{ GeV/cm}^3} \frac{270 \text{ km/s}}{\bar{v}} \frac{1 \text{ GeV}}{m_D} \sum_i F_i(m_D) \frac{\sigma_{N_i}^{\text{SI}}}{10^{-40} \text{ cm}^2} f_i \phi_i S \left( \frac{m_D}{m_{N_i}} \right) \frac{1 \text{ GeV}}{m_{N_i}}$$

$$C_E \approx 10^{-3.5(m_D/\text{GeV})-4} \text{s}^{-1} \frac{\sigma_{\text{H}}^{\text{SI}}}{5 \times 10^{-39} \text{ cm}^2}$$

$$C_A = \frac{\langle \sigma v \rangle}{V_{\text{eff}}}, \quad V_{\text{eff}} = 5.8 \times 10^{30} \text{ cm}^3 \left( \frac{1 \text{ GeV}}{m_D} \right)^{3/2}$$

G. Jungman, M. Kamionkowski, K. Griest  
Phys. Rept. 267, 195 (1996)



## DM annihilation rate in the Sun:

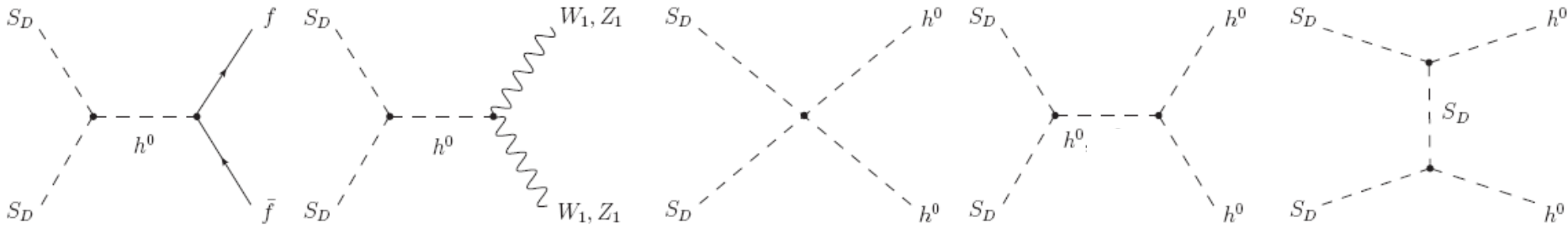
$$\Gamma_{\text{ANN}} = \frac{1}{2} C_A N^2 = \frac{1}{2} C_{\odot} \tanh^2 \left( t_{\odot} \sqrt{C_{\odot} C_A} \right) \gg 1$$

## Total captured DM mass in the Sun:

$$M_{\text{DM}} \sim 2 \times 10^{17} \text{ g}$$

$$M_{\text{Sun}} = 2 \times 10^{33} \text{ g}$$

# The neutrino fluxes at the surface of Earth 15



$$\frac{d\Phi_{\nu_\mu}}{dE_{\nu_\mu}} = \frac{\Gamma_{\text{ANN}}}{4\pi R^2} \frac{dN_{\nu_\mu}}{dE_{\nu_\mu}}$$

$$\frac{dN_{\nu_\mu}}{dE_{\nu_\mu}} = \sum_{fs} B_{fs} \frac{dN_{\nu_\mu}^{fs}}{dE_{\nu_\mu}},$$



- Final state interactions
- Neutrino interactions
- Neutrino oscillations

**WIMPSIM !**

M. Blenow, et. al., 0709.3898

T. Schwetz, et. al., 0808.2016V3

$$\sin^2 \theta_{12} = 0.318, \quad \sin^2 \theta_{23} = 0.50, \quad \sin^2 \theta_{13} = 0.0,$$

$$\Delta m_{21}^2 = 7.59 \times 10^{-5} \text{eV}^2, \quad \Delta m_{31}^2 = 2.40 \times 10^{-3} \text{eV}^2.$$

## Neutrino induced upward muon flux:

$$\Phi_\mu = \int_{E_{\text{thr}}^{\text{SK}}}^{m_D} dE_\mu \int_{E_\mu}^{m_D} dE_{\nu_\mu} \frac{d\Phi_{\nu_\mu}}{dE_{\nu_\mu}} \int_0^\infty dL \int_{E_\mu}^{E_{\nu_\mu}} dE'_\mu g(L, E_\mu, E'_\mu) \sum_{a=p,n} \frac{d\sigma_{\nu_\mu}^a(E_{\nu_\mu}, E'_\mu)}{dE'_\mu} \rho_a$$

+ ( $\nu_\mu \rightarrow \bar{\nu}_\mu$ ),

**$E_{\text{thr}} = 1.6 \text{ GeV}$**

$\rho_p \approx 1/2 N_A \rho$  and  $\rho_n \approx 1/2 N_A \rho$

**Approximation:** T.K. Gaisser and T. Stanev, PRD 30,985 (1984)

$g$  is the probability that a muon of initial energy  $E'_\mu$  has energy  $E_\mu$  after propagating a distance  $L$  in rock.

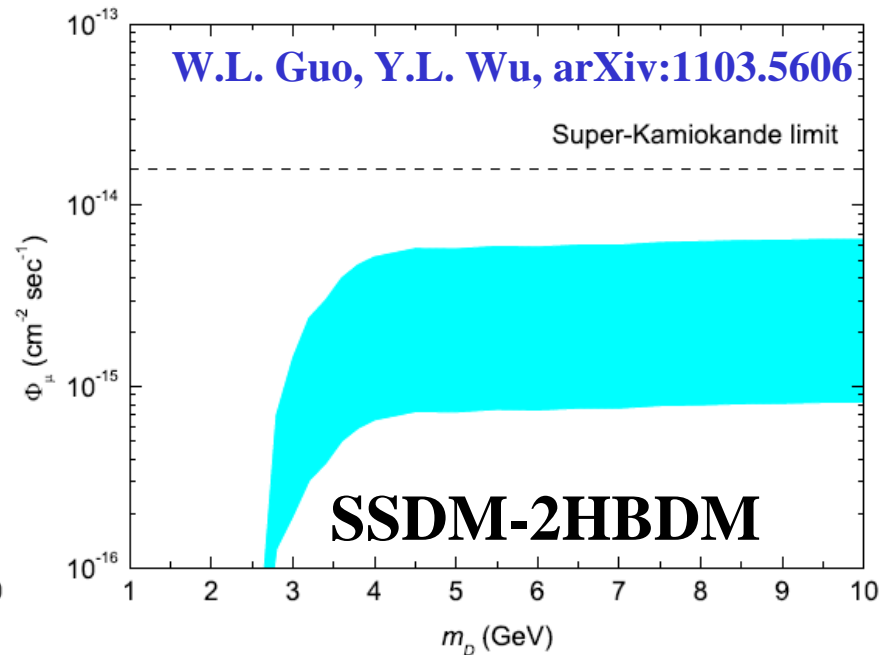
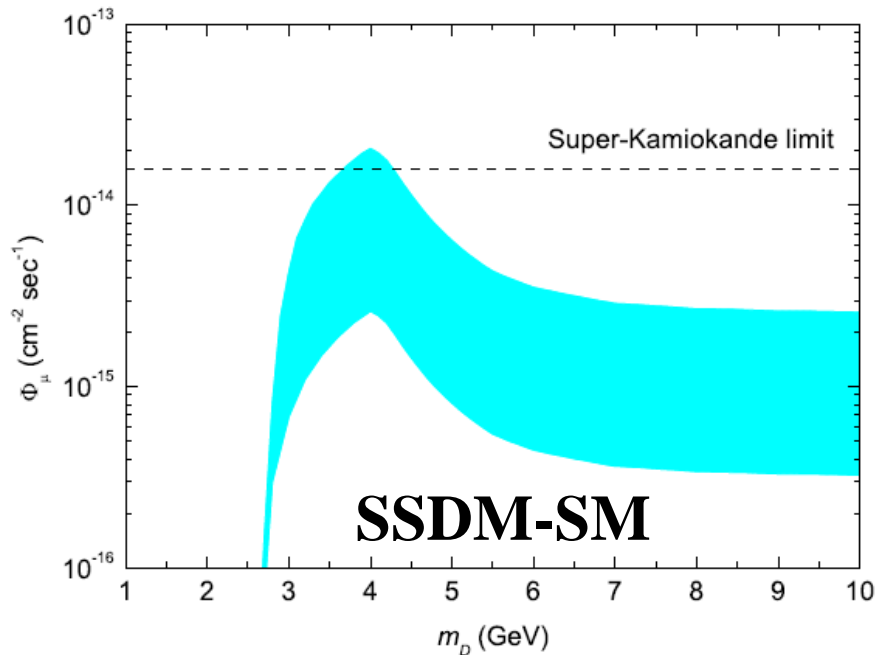
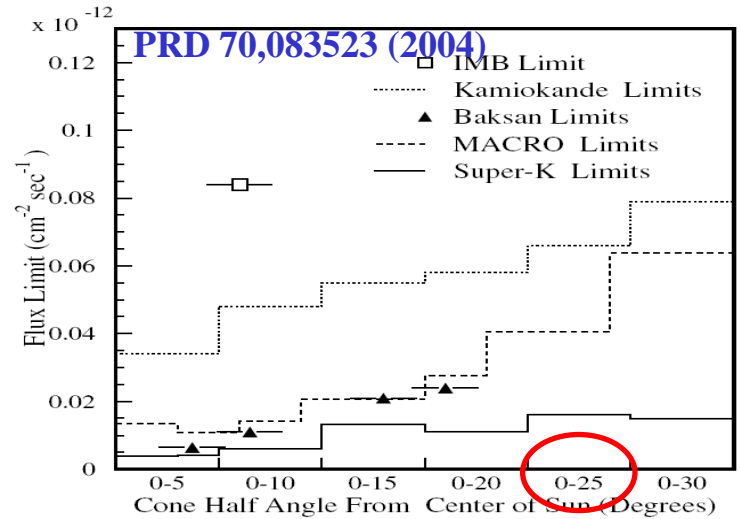
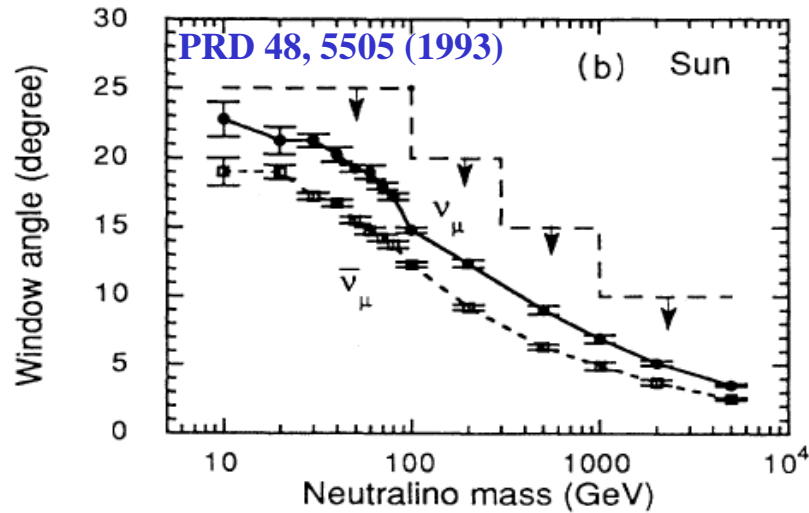
$$g(L, E_\mu, E'_\mu) = \frac{\delta(L - L_0)}{\rho(\alpha + \beta E_\mu)}, \quad L_0 = \frac{1}{\rho\beta} \ln \frac{\alpha + \beta E'_\mu}{\alpha + \beta E_\mu},$$

→

$$\Phi_\mu = \int_{E_{\text{thr}}^{\text{SK}}}^{m_D} dE_\mu \frac{1}{\rho(\alpha + \beta E_\mu)} \int_{E_\mu}^{m_D} dE_{\nu_\mu} \frac{d\Phi_{\nu_\mu}}{dE_{\nu_\mu}} \int_{E_\mu}^{E_{\nu_\mu}} dE'_\mu \sum_{a=p,n} \frac{d\sigma_{\nu_\mu}^a(E_{\nu_\mu}, E'_\mu)}{dE'_\mu} \rho_a + (\nu_\mu \rightarrow \bar{\nu}_\mu).$$

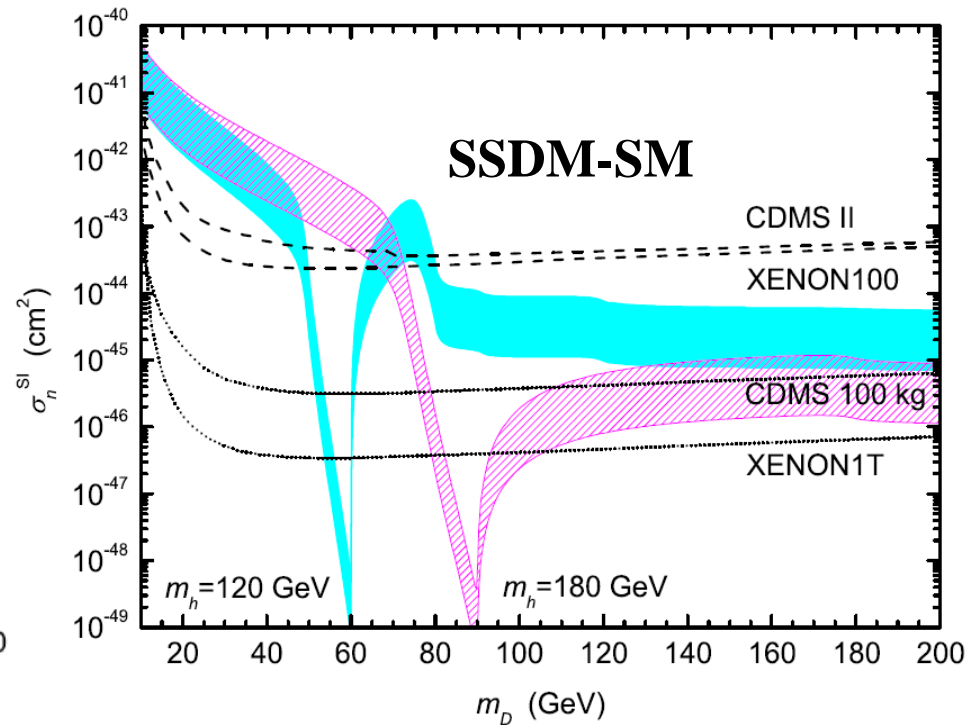
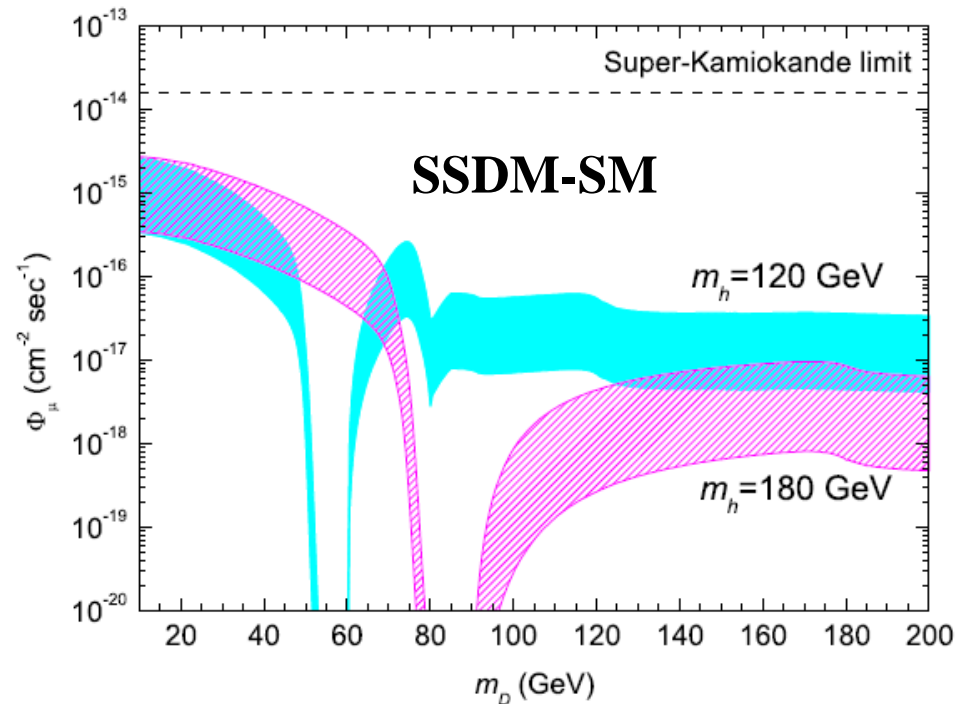


# Super-K results (1)



# Super-K results (2)

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**SSDM-2HBDM!**

Neutrino induced **upward** muon numbers per year :

$$N_\mu = \int_{E_{\text{thr}}^{\text{IC}}}^{m_D} dE_\mu A_{\text{eff}}(E_\mu) \frac{\langle R(\cos \theta_z) \rangle}{2} \frac{1}{\rho(\alpha + \beta E_\mu)} \int_{E_\mu}^{m_D} dE_{\nu_\mu} \frac{d\Phi_{\nu_\mu}}{dE_{\nu_\mu}} \int_{E_\mu}^{E_{\nu_\mu}} dE'_\mu \sum_{a=p,n} \frac{d\sigma_{\nu_\mu}^a(E_{\nu_\mu}, E'_\mu)}{dE'_\mu} \rho_a + (\nu_\mu \rightarrow \bar{\nu}_\mu)$$

$$E_{\text{thr}} = 50 \text{ GeV}$$

$$\rho_p \approx 5/9 N_A \rho \text{ and } \rho_n \approx 4/9 N_A \rho$$

Effective area:

M.C. Gonzalez-Garcia, F. Halzen, S. Mohapatra, 0902.1176

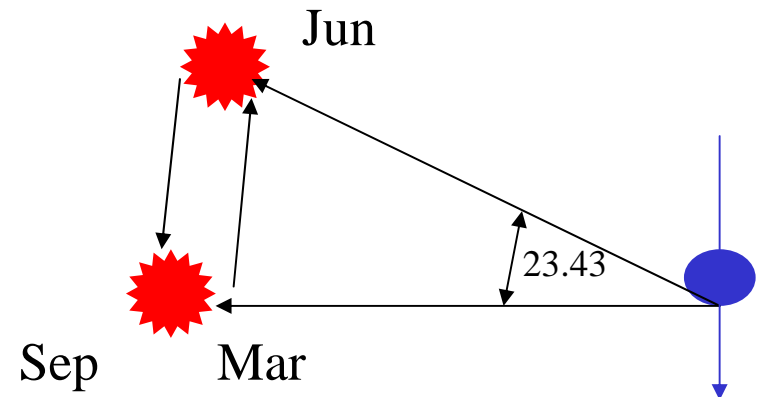
$$A_{\text{eff}}(E_\mu \leq 10^{1.6} \text{ GeV}) = 0,$$

$$A_{\text{eff}}(10^{1.6} \text{ GeV} < E_\mu < 10^{2.8} \text{ GeV}) = 0.748 [\log(E_\mu / \text{GeV}) - 1.6] \text{ km}^2,$$

$$A_{\text{eff}}(E_\mu \geq 10^{2.8} \text{ GeV}) = 0.9 + 0.54 [\log(E_\mu / \text{GeV}) - 2.8] \text{ km}^2.$$

Average R:

$$R(\cos \theta_z) = 0.92 - 0.45 \cos \theta_z$$



# Atmosphere Background

Atmosphere Background:  $\left\langle \frac{d\Phi_{\nu\mu}}{dE_{\nu\mu}}(\cos\theta_z)R(\cos\theta_z) \right\rangle$

TABLE XXII.  $\nu_\mu$  flux ( $\text{m}^{-2} \text{sec}^{-1} \text{sr}^{-1} \text{GeV}^{-1}$ ) above 10 GeV.

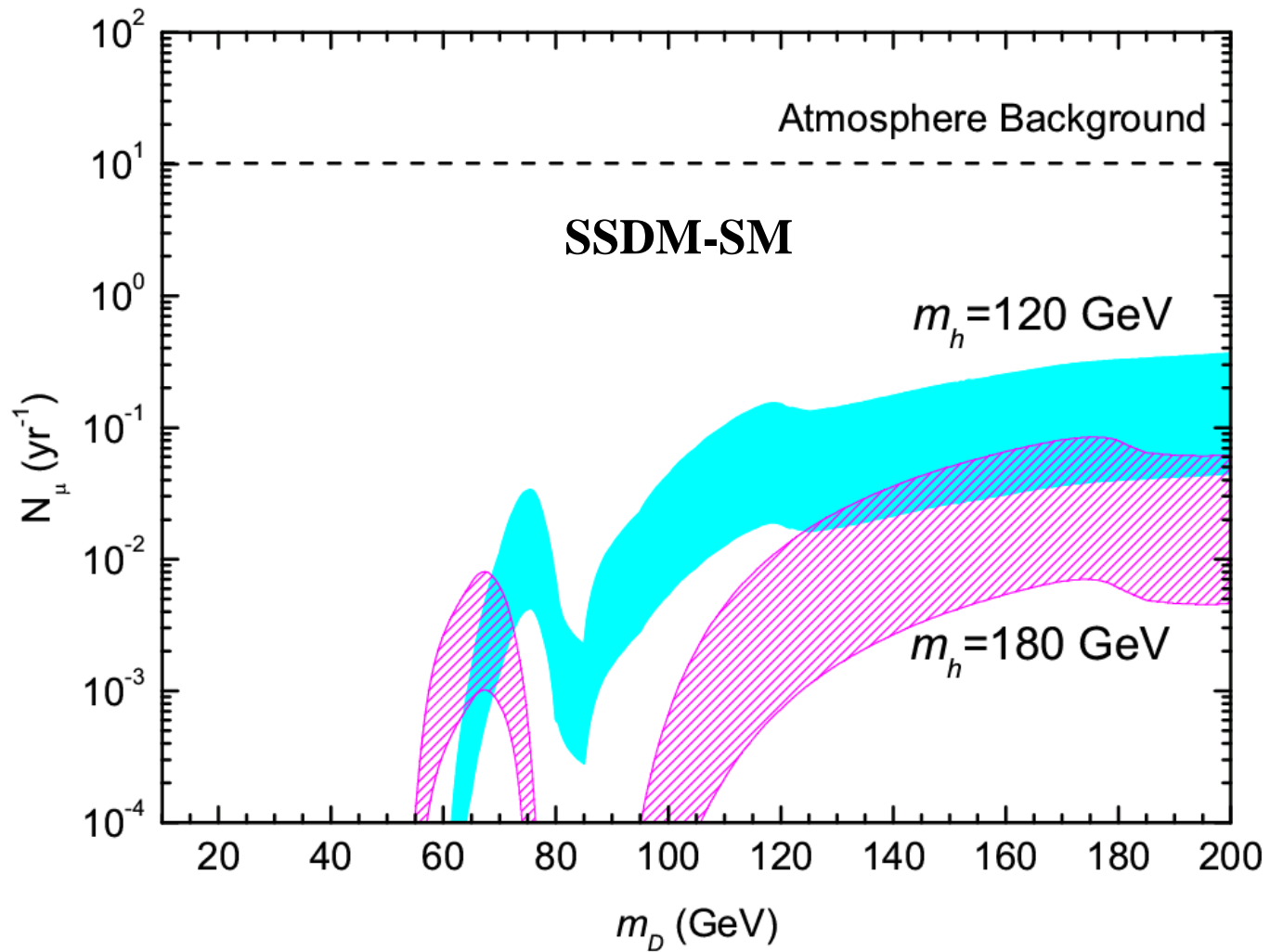
| $E_\nu$ (GeV)       | $\cos\theta_z$ |       |       |       |       |       |       |       |       |       | <i>Norm</i> |
|---------------------|----------------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------------|
|                     | 1.-.9          | .9-.8 | .8-.7 | .7-.6 | .6-.5 | .5-.4 | .4-.3 | .3-.2 | .2-.1 | .1-.0 |             |
| $1.000 \times 10^1$ | 2.557          | 2.625 | 2.703 | 2.799 | 2.911 | 3.052 | 3.232 | 3.482 | 3.824 | 4.172 | $10^{-1}$   |
| $1.259 \times 10^1$ | 1.295          | 1.331 | 1.370 | 1.419 | 1.479 | 1.554 | 1.646 | 1.778 | 1.964 | 2.166 | $10^{-1}$   |
| $1.585 \times 10^1$ | 0.654          | 0.673 | 0.694 | 0.720 | 0.751 | 0.789 | 0.840 | 0.906 | 1.009 | 1.121 | $10^{-1}$   |
| $1.995 \times 10^1$ | 3.297          | 3.397 | 3.505 | 3.653 | 3.811 | 4.001 | 4.269 | 4.612 | 5.154 | 5.807 | $10^{-2}$   |
| $2.512 \times 10^1$ | 1.659          | 1.710 | 1.770 | 1.848 | 1.930 | 2.033 | 2.167 | 2.349 | 2.627 | 2.997 | $10^{-2}$   |
| $3.162 \times 10^1$ | 0.831          | 0.858 | 0.891 | 0.931 | 0.974 | 1.033 | 1.100 | 1.197 | 1.340 | 1.542 | $10^{-2}$   |
| $3.981 \times 10^1$ | 4.144          | 4.291 | 4.463 | 4.663 | 4.898 | 5.205 | 5.572 | 6.091 | 6.852 | 7.935 | $10^{-3}$   |
| $5.012 \times 10^1$ | 2.055          | 2.136 | 2.225 | 2.329 | 2.457 | 2.612 | 2.819 | 3.085 | 3.482 | 4.051 | $10^{-3}$   |
| $6.310 \times 10^1$ | 1.014          | 1.056 | 1.104 | 1.161 | 1.228 | 1.308 | 1.420 | 1.556 | 1.762 | 2.059 | $10^{-3}$   |
| $7.943 \times 10^1$ | 0.499          | 0.519 | 0.545 | 0.576 | 0.609 | 0.653 | 0.710 | 0.783 | 0.897 | 1.054 | $10^{-3}$   |
| $1.000 \times 10^2$ | 2.443          | 2.551 | 2.679 | 2.838 | 3.012 | 3.248 | 3.541 | 3.930 | 4.524 | 5.345 | $10^{-4}$   |
| $1.259 \times 10^2$ | 1.194          | 1.253 | 1.315 | 1.394 | 1.487 | 1.606 | 1.761 | 1.967 | 2.259 | 2.676 | $10^{-4}$   |
| $1.585 \times 10^2$ | 0.583          | 0.611 | 0.643 | 0.684 | 0.732 | 0.790 | 0.869 | 0.979 | 1.129 | 1.338 | $10^{-4}$   |
| $1.995 \times 10^2$ | 2.837          | 2.969 | 3.134 | 3.340 | 3.568 | 3.876 | 4.270 | 4.843 | 5.619 | 6.676 | $10^{-5}$   |
| $2.512 \times 10^2$ | 1.371          | 1.439 | 1.521 | 1.621 | 1.732 | 1.897 | 2.092 | 2.384 | 2.785 | 3.322 | $10^{-5}$   |
| $3.162 \times 10^2$ | 0.658          | 0.695 | 0.737 | 0.786 | 0.844 | 0.923 | 1.022 | 1.168 | 1.378 | 1.646 | $10^{-5}$   |
| $3.981 \times 10^2$ | 3.146          | 3.328 | 3.547 | 3.792 | 4.096 | 4.482 | 4.988 | 5.700 | 6.771 | 8.124 | $10^{-6}$   |
| $5.012 \times 10^2$ | 1.496          | 1.585 | 1.696 | 1.819 | 1.975 | 2.171 | 2.425 | 2.776 | 3.308 | 3.990 | $10^{-6}$   |
| $6.310 \times 10^2$ | 0.706          | 0.753 | 0.806 | 0.869 | 0.949 | 1.045 | 1.172 | 1.353 | 1.617 | 1.950 | $10^{-6}$   |
| $7.943 \times 10^2$ | 3.307          | 3.537 | 3.807 | 4.123 | 4.521 | 5.008 | 5.643 | 6.568 | 7.855 | 9.512 | $10^{-7}$   |
| $1.000 \times 10^3$ | 1.535          | 1.643 | 1.781 | 1.940 | 2.133 | 2.386 | 2.708 | 3.167 | 3.796 | 4.634 | $10^{-7}$   |
| $1.259 \times 10^3$ | 0.705          | 0.759 | 0.825 | 0.905 | 1.001 | 1.125 | 1.288 | 1.515 | 1.840 | 2.250 | $10^{-7}$   |
| $1.585 \times 10^3$ | 0.320          | 0.347 | 0.378 | 0.418 | 0.465 | 0.526 | 0.608 | 0.722 | 0.886 | 1.088 | $10^{-7}$   |
| $1.995 \times 10^3$ | 1.441          | 1.568 | 1.717 | 1.908 | 2.141 | 2.439 | 2.848 | 3.416 | 4.222 | 5.239 | $10^{-8}$   |
| $2.512 \times 10^3$ | 0.643          | 0.702 | 0.775 | 0.861 | 0.973 | 1.119 | 1.318 | 1.597 | 2.007 | 2.511 | $10^{-8}$   |
| $3.162 \times 10^3$ | 0.285          | 0.312 | 0.346 | 0.387 | 0.438 | 0.508 | 0.605 | 0.742 | 0.945 | 1.197 | $10^{-8}$   |
| $3.981 \times 10^3$ | 1.251          | 1.375 | 1.530 | 1.724 | 1.965 | 2.286 | 2.757 | 3.422 | 4.400 | 5.675 | $10^{-9}$   |
| $5.012 \times 10^3$ | 0.548          | 0.602 | 0.675 | 0.759 | 0.878 | 1.024 | 1.243 | 1.553 | 2.047 | 2.670 | $10^{-9}$   |
| $6.310 \times 10^3$ | 0.238          | 0.264 | 0.296 | 0.335 | 0.389 | 0.457 | 0.556 | 0.706 | 0.944 | 1.237 | $10^{-9}$   |
| $7.943 \times 10^3$ | 1.032          | 1.156 | 1.284 | 1.473 | 1.694 | 2.021 | 2.466 | 3.196 | 4.304 | 5.676 | $10^{-10}$  |
| $1.000 \times 10^4$ | 0.444          | 0.497 | 0.556 | 0.635 | 0.732 | 0.882 | 1.079 | 1.410 | 1.946 | 2.615 | $10^{-10}$  |

Take half-angle to be 2 degree!

$E_{\mu}$  from 50 to 200 GeV



10.2 yr<sup>-1</sup>



- ❖ The current DM direct search experiments can exclude parts of parameter space:  $f > 0.63$  ( $m_D < 10$ ),  $8 < m_D < 50 \text{ GeV}$ .....
- ❖ The predicted muon fluxes in  $3.7 < m_D < 4.2 \text{ GeV}$  and  $f > 0.65$  slightly exceed the SK limit. The CDMS excludes this region.
- ❖ For the SSDM-2HBDM, one can adjust the Yukawa couplings to avoid the direct detection limits and enhance the predicted muon fluxes.
- ❖ For the allowed parameter space of SSDM-SM and SSDM-2HBDM, the predicted muon fluxes in Super-K and the muon event rates in IceCube are less than the Super-K limits and atmosphere background, respectively.

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**Thanks !**